

EE 201.3 (Section 03)

(Instructor: Denard Lynch)

Midterm Examination

Tuesday, October 26, 2004

7:00 PM

Time Allowed: 2 Hours

**Materials allowed: One 8½" X 11" formula sheet,
Calculators**

Instructions:

- Answer all questions in the space provided (use page backs for rough work if necessary)
- State your assumptions; show all relevant work. Box, circle, or otherwise highlight your answers.
- Put your name and student number on the cover page; put *only* your student number on all remaining pages.
- Weighting for each question is indicated in the left margin (Total marks: 50)

| 1 | 2 | 3 | 4 | 5 | 6 | Total |
|---|---|---|---|---|---|-------|
| / | / | / | / | / | / | / |

Name: _____

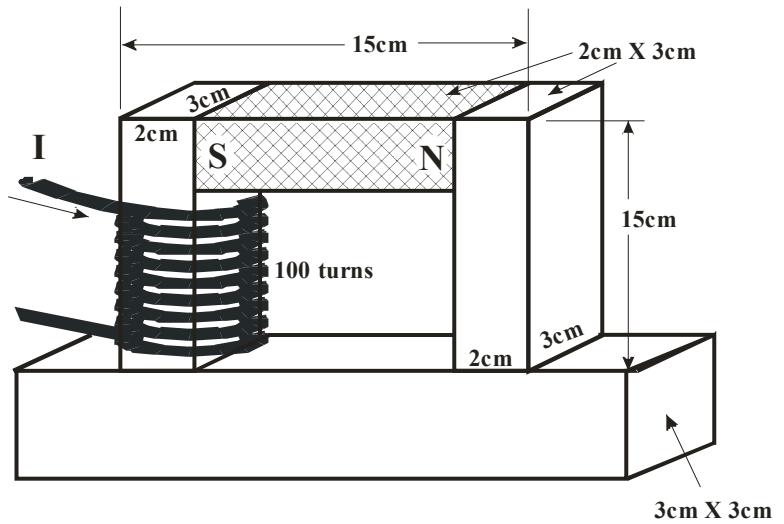
Student Number: _____

1) State Ohm's Law for Magnetic circuits: _____

[1]

2) The magnet shown in the figure is used to pick up sheet steel bars and place them on a conveyor for milling.

The centre section is a permanent magnet that provides an mmf of 500A-t, and has an internal reluctance of 250,000 A-t/Wb (which can be assumed constant). The end sections are the same 2cm x 3cm. cross section as the permanent magnet, and are made out of cast steel. One of the legs has a coil of 100 turns wound in the direction shown.



$$\text{Note: } F = \frac{B_{\text{gap}}^2 A_{\text{gap}}}{2\mu_0}$$

Assume there is no gap between the magnet and the bar. (B-H curves are on the last page)

Answer the following questions about this magnet system:

a) Draw the electric equivalent of the magnetic circuit.

[2]

b) What is the minimum flux that must be flowing in the magnet if it is to hold up a bar with a mass of 50Kg?

[2]

(Note: You may use the following table to assist with your calculations)

| Leg | Φ (Wb) | A (m^2) | B (T) | H (At/m) | L (m) | HI (At) | | |
|-----|-------------|----------------------|---------|------------|---------|-----------|--|--|
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c) Assuming *no current* flowing in the coil, will the permanent magnet generate enough flux in this circuit to hold up the bar?

[4]

d) What is the magnitude and direction of the current required in the coil at the point when the bar will drop?

[4]

e) What is the inductance of the coil at the point where the bar just "lets go"?

[2]

3) What is the period of a sinusoidal waveform that completes 360 cycles in 42msec?

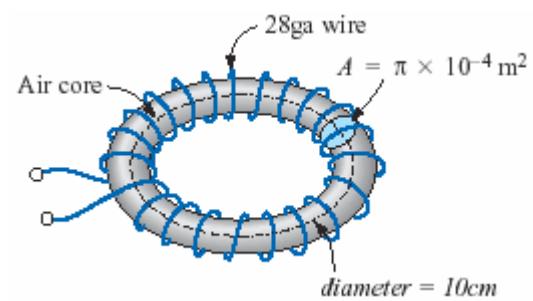
[1]

$$T = \text{_____}.$$

4) The $12.5\mu\text{H}$ air-core inductor shown in the figure consists of 28 gauge copper wire. The toroid has a diameter of 10cm and a cross-sectional area of $\pi \times 10^{-4}\text{m}^2$.

[3]

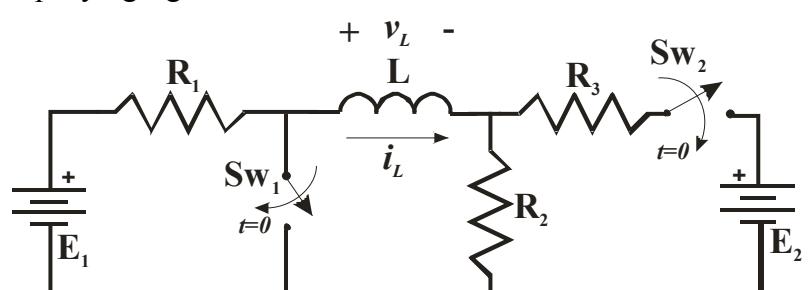
a) How many turns are in the coil?



5) Consider the R – L circuit in the accompanying figure.

(Note the defined polarity of v_L and direction of i_L)

Assume that the system has reached steady-state before both the switches, Sw_1 and Sw_2 , are closed at exactly the same time.



Answer the questions below given the following circuit parameters:

$$E_1=10\text{V}, E_2=12\text{V}, R_1=100\Omega, R_2=33\Omega, R_3=470\Omega, \text{ and } L=0.3\text{H}$$

a) Find v_L and i_L before the switches are closed.

[2]

b) How much energy is stored in the inductor *before* the switches are closed?

[1]

Answer the remaining questions assuming the switches are closed at $t = 0$.

c) What is the time constant, τ , in the R-L circuit *after* the switches are closed?

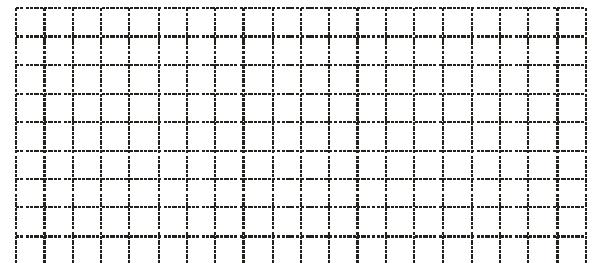
[2]

d) What will the final steady-state current be through the inductor?

[2]

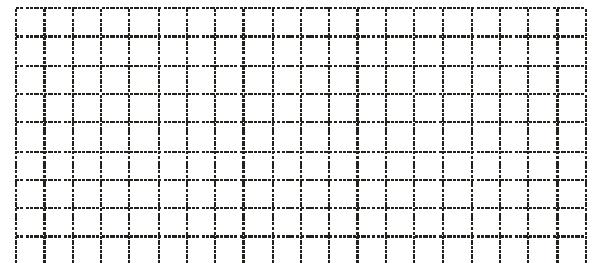
e) Write the expression and graph the waveform for the current i_L as a function of time.

[3]



f) Find the expression and graph the waveform for the voltage, v_L as a function of time.

[3]



g) At what time will $i_L = 0$?

[3]

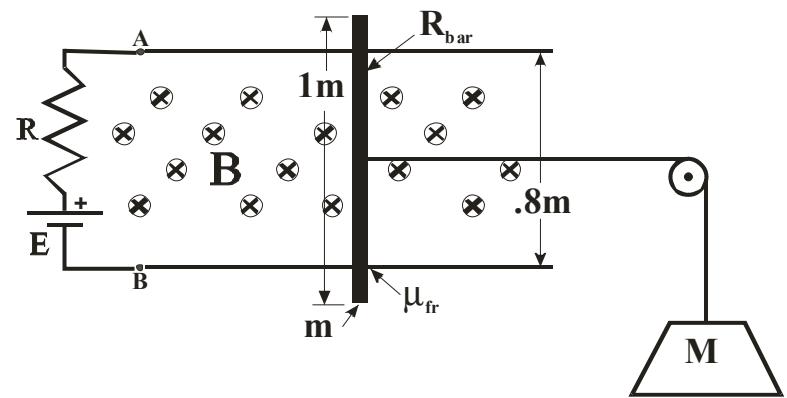
6) If we consider fringing effects, the *effective area* at air gap 1mm long in a circular cross-section with a diameter of 2cm is:

[1]

i) 3.80×10^{-3} ii) 3.14×10^{-4} iii) 3.80×10^{-4} iv) 1.39×10^{-3}

7) Consider the following Bar & Rail system attached to a voltage source and mass as shown in a magnetic field of density, B. The system consists of a **1m long** bar of mass, **m = 10.0kg** which is in contact with two rails which are **0.8meters** apart.

The bar is connected to a mass **m = 5kg** through a cable and pulley so that the mass can travel vertically. The coefficient of static friction, μ_{fr} between the bar and the rails is **0.3**. A battery with a terminal voltage, **E = 24V** is connected through a resistor, **R**, to the rails at points **A** and **B**. The resistance of the bar, **$R_{bar} = 0.1\Omega$** .



a) Assuming the bar is at rest, what is the *direction* of the magnetic force acting on the bar? (left or right or up or down)

[1]

Assume the system has reach steady state for the remaining questions.

b) The bar is moving to the right with a velocity of 34 m/s. What flux density, B, is present if a motional emf of 30V is observed *in the bar*?

[1]

c) With this flux density, how much current is flowing in the bar and what is its direction (*up* or *down* through the bar)?

[2]

d) What is the value of the external resistor, R ?

[2]

e) What is V_{AB} ?

[2]

f) Is the bar & Rail system acting as a *motor* or *generator*?

[1]

g) What is the total power into the system (in Watts) and what is the source?

[1]

h) What is the useful power out of the system and where does it go?

[1]

i) What is the efficiency, η , of the whole system?

[1]

8) What is the voltage across a 100mH inductor if the current through it is charging at a rate of $1\text{mA}/\mu\text{s}$.

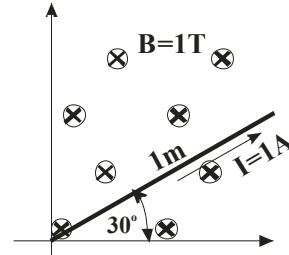
[1]

i) 0V ii) 1V iii) 100V

9) What is the magnitude of the force on the wire shown in the diagram if it is carry a current of 1A ?

[1]

i) 1N
ii) 0.5 N
iii) 0.87 N



Some potentially useful constants:

Acceleration of gravity: $g = 9.81 \text{ m/s}^2$

Permeability of free space: $\mu_0 = 4\pi \times 10^{-7} \text{ Wb/At-m}$

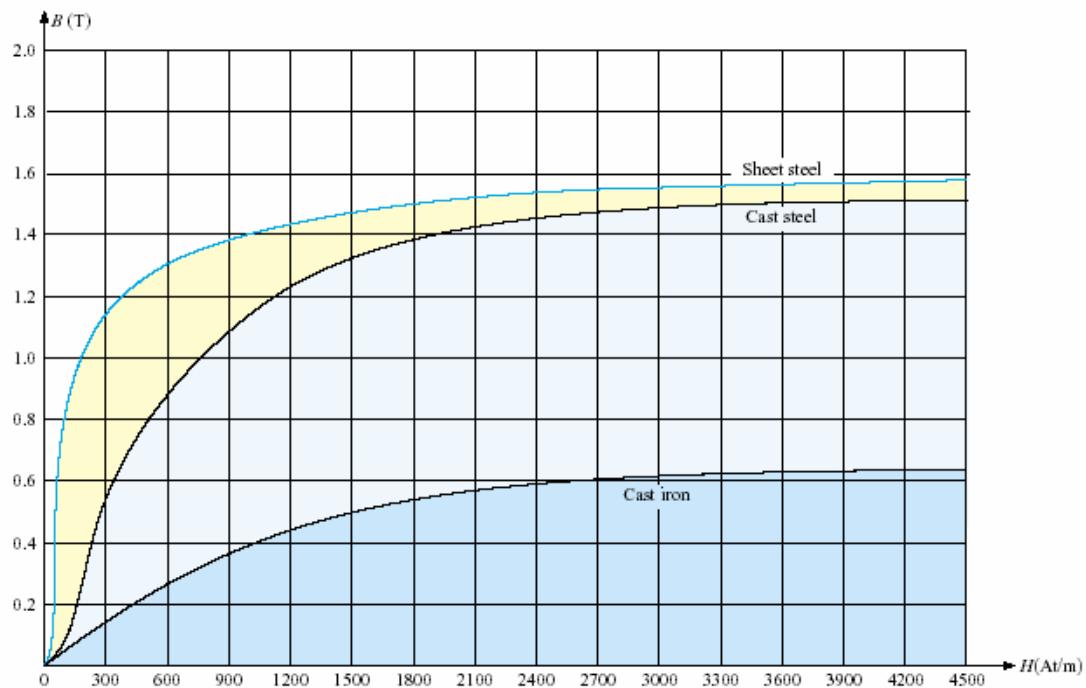


FIG. 11.23
Normal magnetization curve for three ferromagnetic materials.

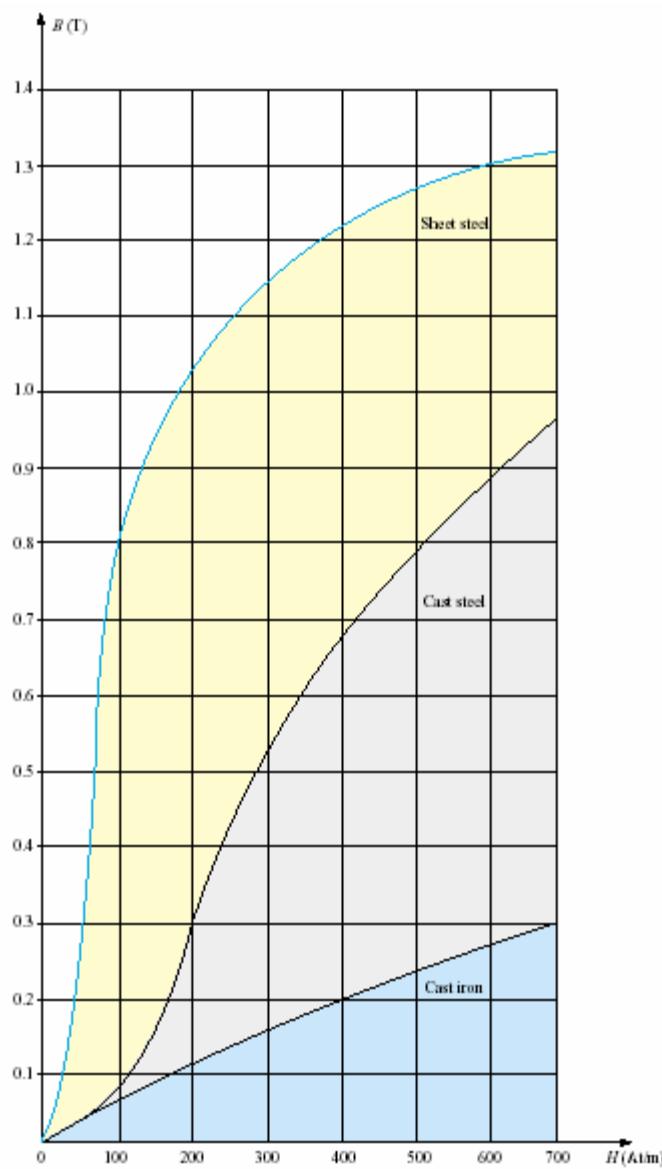


FIG. 11.24
Expanded view of FIG. 11.23 for the low magnetizing force region.

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